

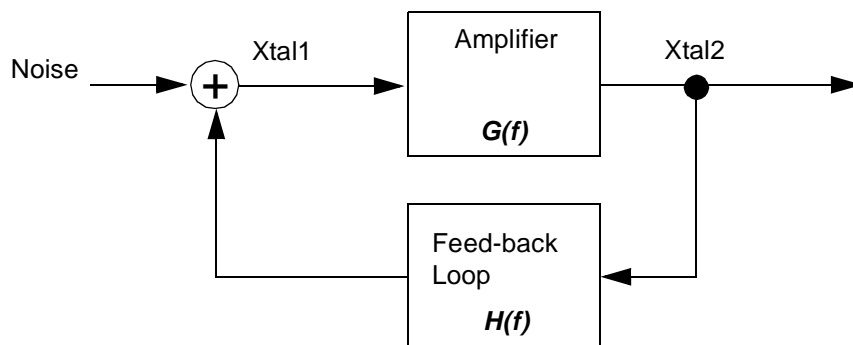
Analyzing the Behavior of an Oscillator and Ensuring Good Start-up

This application note explains how an oscillator functions and which methods can be used to check if the oscillation conditions are met in order to ensure a good start-up when power is applied.

Oscillator Fundamentals

A microcontroller integrates on-chip an oscillator to generate a stable clock used to synchronize the CPU and the peripherals.

Figure 1. Basic Oscillator Architecture



The basic architecture of an oscillator (regardless of its structure) is shown in Figure 1 and built around an amplifier, a feed-back and noise applied on Xtal1 input. The role of each elements is explained hereafter:

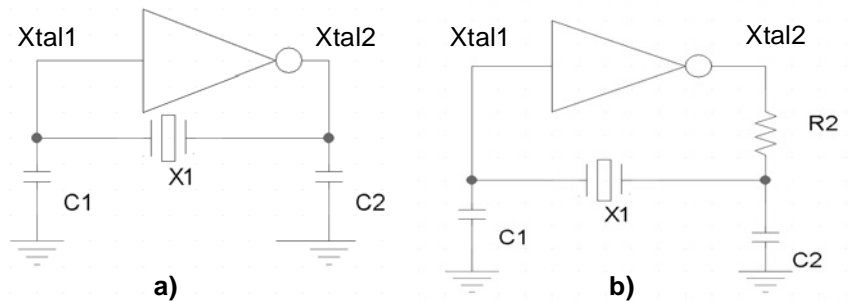
- **Amplifier:** Used to amplify the signal applied on Xtal1 and to lock the oscillations exhibit Xtal2. The class A structure is the most popular but new ones are currently used in order to optimize the consumption or other criterion,
- **Feed-back loop:** Used to filter the output signal and to send it to the Xtal1 input. The oscillator stability is linked to the bandwidth of the loop. The narrower the filter, the more stable the oscillator. Crystals or ceramic resonators are generally used because they have the narrowest bandwidth and efficiency for the stability of the frequency.

- **Noise:** Thanks to the noise an oscillator is able to startup. This noise has different origins:
 - **thermal noise** due to the transistor junctions and resistors,
 - **RF noise:** a wide band noise is present in the air and consequently on all the pins of the chip and in particular on Xtal1 input of the amplifier. The noise origin can be industrial, astronomic, semiconductor, ...
 - **transient noise** during the power-up.

The noise is coupled to the amplifier from the inside and outside of the chip through the package, the internal power rails,

Figure 2 shows the typical oscillator structure used in most microcontroller chips. An on-chip amplifier connected to an external feed-back consists in a crystal or a resonator and two capacitors (a). Sometimes a resistor is inserted (b) between the amplifier output and the crystal in order to limit the power applied, avoiding the destruction of the crystal.

Figure 2. Typical Oscillator Structures

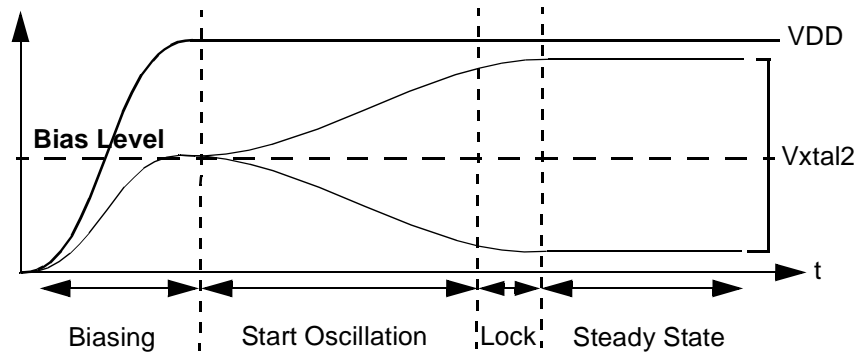


Typical Oscillator Operation

The process involved in start-up and locking of oscillator is explained hereafter (see Figure 3):

- **Biasing process.** The power-up is applied and the amplifier output follows the power until it reaches its biasing level where it can amplify the noise signal on its input.
- **Oscillation.** The amplified noise on the output (*Xtal2*) is filtered by the feed-back loop which has a pass-band frequency corresponding to the nominal oscillator frequency. The filtered output noise is amplified again and starts to increase. The oscillation level continues to grow and reaches the non-linear area.
- **Lock.** In the non-linear area both the gain and the oscillation level starts to reduce.
- **Steady State.** A stabilization point is found where the closed-loop gain is maintained with the unity.

Figure 3. Process Needed to Reach a Stable Oscillation



Each element plays a role and their electrical characteristics have to be understood. The next sections explain this matter.

Crystal Model and Operation

Crystal and ceramic resonators are piezoelectric devices which transform voltage energy to mechanical vibrations and vice-versa. At certain vibrational frequencies, there is a mechanical resonance. Main resonances are called: fundamental, third, fifth, ... overtones. Overtones are not harmonics but different mechanical vibrational modes.

This crystal is an efficient pass-band filter which exhibits a good frequency stability. The equivalent model, shown in Figure 4, consists of two resonant circuits:

- **C1, L1** and **R1** is a series resonant circuit (**fs**),
- In addition the series circuit, **C0** in parallel forms a parallel circuit which has a parallel resonance frequency (**fa**).

Figure 4. Crystal Models.

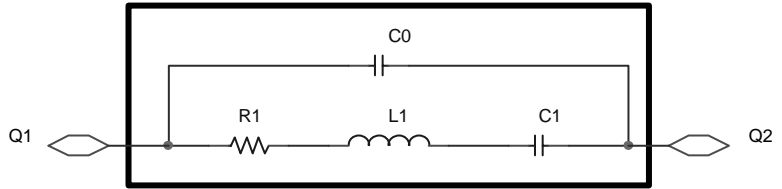
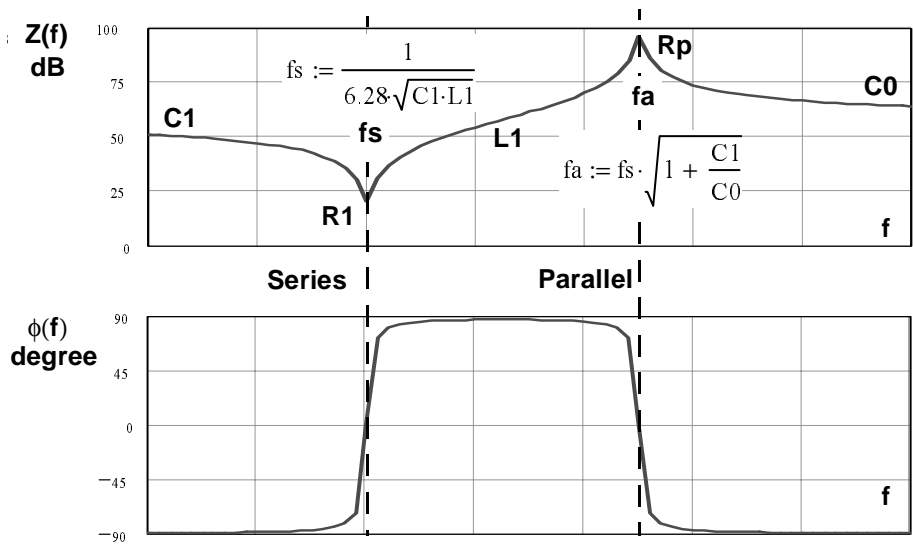


Figure 5 plots the module and phase of the impedance crystal and shows both the series and parallel resonance frequencies.

Figure 5. Phase and Module Versus the Frequency



The behavior of the crystal depends on the frequency and is summarized in Table 1.

Table 1. Nature of the Impedance Versus the Frequency

Frequency	$f < f_s$	$f = f_s$	$f_s < f < f_a$	$f = f_a$	$f > f_a$
Z(f)	Capacitive C1	Resistance R1	Inductive L1	Resistance Rp	Capacitive C0
Phase(°)	-90	0	+90	0	-90

The impedance phase is related to the frequency and each elements of the model plays a role in specific frequency ranges. The main electrical characteristics of these elements are summarized hereafter.

Series resonance frequency $f_s := \frac{1}{6.28\sqrt{C1 \cdot L1}}$ **Quality factor** $Q_s := \frac{L1 \cdot 6.28 f_s}{R1}$

Parallel resonance

frequency $f_a := f_s \cdot \sqrt{1 + \frac{C1}{C0}}$ **Quality factor** $Q_p := \frac{1}{C0 \cdot 6.28 f_p \cdot R1}$

With External Load, CL

frequency $f_p := f_s \cdot \left[1 + \frac{C1}{2 \cdot (C0 + CL)} \right]$ **ESR** $ESR := R1 \cdot \left(1 + \frac{C0}{CL} \right)^2$

Quality factor $Q_p := \frac{1}{CL \cdot 6.28 f_p \cdot ESR}$

Table 2 gives some typical crystal characteristics.

Table 2. Examples of Crystal Characteristics

Frequency MHz	R1 ohms	L1 mH	C1 fF	C0 pF	fs MHz	fp MHz	Qs	Qp
32	35	11.25	2.2	7	32	32.005	646k	3.11
30 ⁽²⁾	20	11	2.6	6	30	30.0065	102k	6.14
30 ⁽¹⁾	40	33.94	0.83	3.8	30	30.00328	160k	3.48
20	50	20	3.2	10	20	20.0032	497k	2.98
16	80	11.641	8.5	3	16	16.022	146k	3.42
10	20	0.025	10	20	10	10.00025	159.2k	80
8	7	0.0862	4.6	40	8	8.00026	618k	17.4
6	8	0.0848	8.3	40	6	6.000356	533k	37
2	100	520	12	4	2	2.003	66K	198

- Note: 1. Fundamental Mode
2. Third Overtone Mode

“Series” Versus “Parallel” Crystal

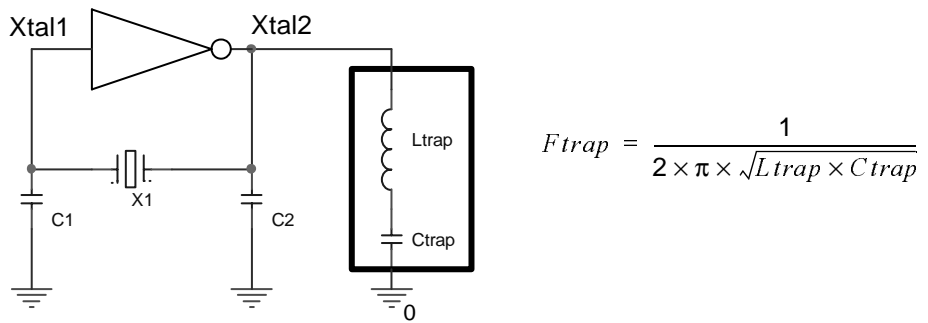
There is no such thing as a “series cut” crystal as opposed to a “parallel cut” crystal. Both modes exist in a crystal. Only the oscillator structures (Pierce, Colpitts, ..) will oscillate the crystal close to the **fs** or between **fs** and **fa** resonance frequencies. The first structure is called a **series resonant oscillator** and the second a **parallel resonant oscillator**. It should be noted that no oscillator structure is able to oscillate at the exact **fa** frequency. This is due to the high quality factor at **fa** and the difficulty to stabilize an oscillator at this frequency.



Overtone or Fundamental Mode

Vibrational mode is used to reduce the crystal cost. Above 20MHz it is costly to produce such crystals tuned on the fundamental mode. To avoid that, an overtone mode is used to tune the oscillation frequency. To work properly, this vibrational mode needs a specific schematic where a frequency trap is installed on the oscillator output to short-circuit the fundamental mode and force the overtone mode. The trap is an LC filter installed between the **Xtal2** and the ground. The frequency on this filter is calculated on the fundamental mode using the Thomson equation (see Figure 6).

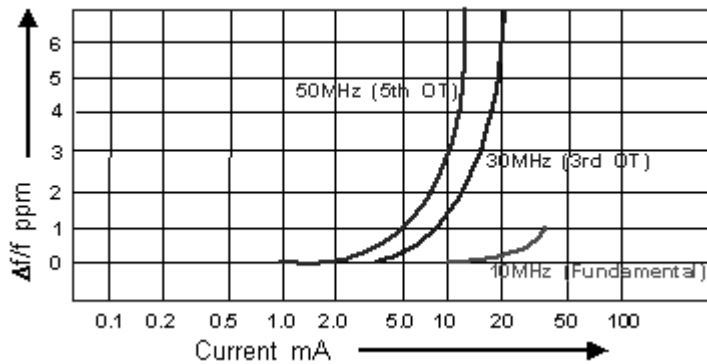
Figure 6. A LC trap is Used for an Overtone Oscillator



Drive Level

The characteristics of quartz crystals are influenced by the drive level. In particular, when the drive level increases, the frequency and the resistance change through non-linear effects. In extreme cases an inharmonic mode may replace the main mode as the selective element and cause the frequency of the oscillator jump to a different frequency. With an overdrive level, the crystal substrate itself may be damaged. Typical characteristic of frequency vs. drive levels is shown in Figure 7.

Figure 7. Frequency Shift vs. Drive Level



Drive level is a measurement of the total power dissipated through the crystal operating in the circuit. Typical drive levels are between 50 uW and 1000 uW (1 mW). Drive levels should be kept at the minimum level that will initiate and maintain oscillation. It should be less than half of the maximum drive level. Excessive drive may cause correlation difficulties, frequency drift, spurious emissions, "ringing" wave forms, excessive ageing, and/or fatal structural damage to the crystal.

The maximum drive, **PMax**, is specified by the crystal manufacturer. The maximum RMS current which can flow in the crystal and it is given by the following expression:

$$PM_{rms} := ESR \cdot IM_{rms}^2 \quad IM_{rms} := \sqrt{\frac{PM_{rms}}{ESR}}$$

where **ESR** is equivalent resistance at the parallel frequency, **fp**.

For example, 0.1 Watt Maximum power with an ESR of 32 ohms gives a 56mA maximum RMS current.

The RMS voltage across the crystal can be evaluated in the same manner:

$$UM_{rms} := \sqrt{PM_{rms} \cdot ESR}$$

where **UMrms** is the maximum RMS value.

For example, if **PMrms** is 0.1Watt and ESR =32Ohms, the maximum RMS voltage across the crystal is 1.8V. In case of overdrive power, a resistor must be connected between the amplifier output and the crystal as shown in Table 2.

Class-A Amplifier

Figure 8 gives an example of a class-A amplifier. Resistance **Rf** is used to bias the output stage to VDD/2. **Cxtal1** and **Cxtal2** are the parasitic capacitors due to input and output amplifier pads plus the parasitic capacitances of the package. **Rout** is the equivalent output resistance of the amplifier. The equivalent schematic is true only for the linear area of the gain and for small signal conditions. This linear operation occurs during the startup when the power is applied. The transfer function is often first order and low-pass filter type.

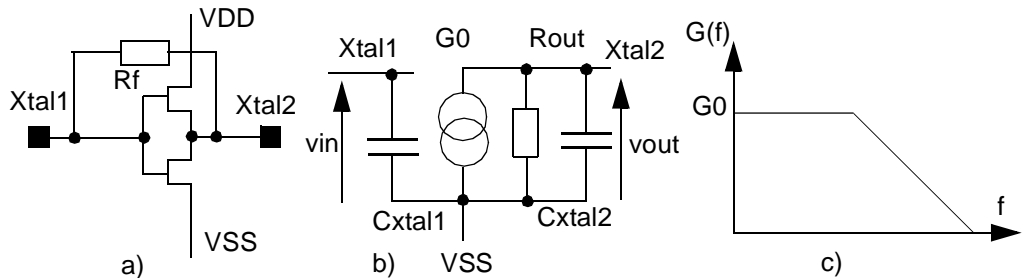


Figure 8. (a) Typical structure of a class-A amplifier. (b) Equivalent schematic. (c) Gain response.

Next section explains the two specific amplifier areas needed to startup and lock an oscillator.

The Two Operating Areas

Figure 9 illustrates the transfer function of a CMOS amplifier. An amplifier such as that shown in Figure 8 has two operating regions. These regions determine the oscillator operation at start-up and during steady state while oscillations are stabilized. Figure 9 shows these two regions:

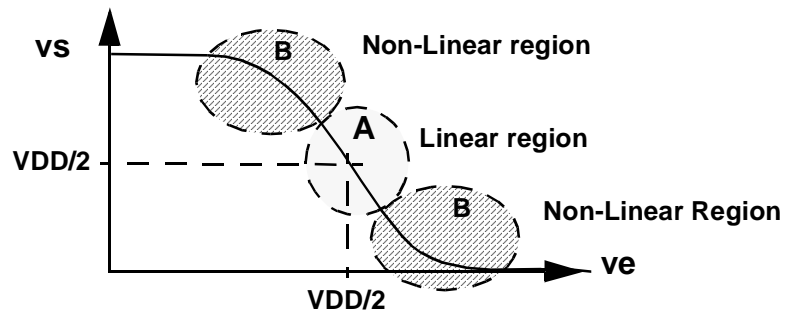
- **Region A, is the linear region.** The gain is constant, and **vout** is proportional to **vin**:

$$v_{out}(f) = G(f) \times v_{in}(f)$$

The dynamic range of this linear region is typically +/- 1 volt around the quiescent point Q at 5v VDD.

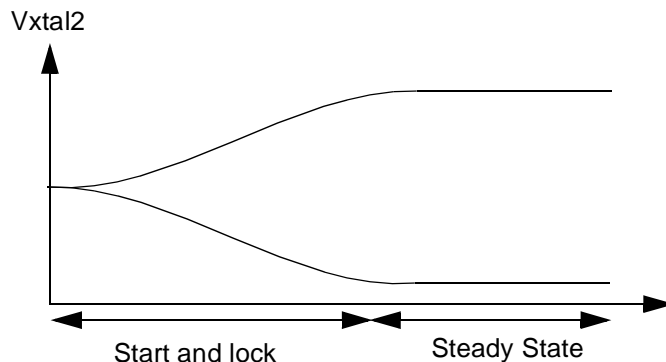
- **Region B, is the non-linear region.** The gain is no longer linear, and becomes dependent on the **vout level**. The higher the **vout**, the lower the gain. The amplification is automatically reduced while the output oscillation increases until a stabilization point is found (amplitude limitation).

Figure 9. Gain Curve and the Two Amplification Region



The oscillations start gradually. The noise on its input is amplified until the level reaches VDD. If conditions (gain and phase) as specified above are fulfilled, startup is normally guaranteed at circuit power-on time. Indeed, during power-on, noise over a large spectrum appears and is sufficient to start-up the system. Only a few microvolts or millivolts are needed but the startup time is inversely proportional to this level. Typical waveform of an oscillation is shown in Figure 10.

Figure 10. Start and Lock of a Feedback Oscillator



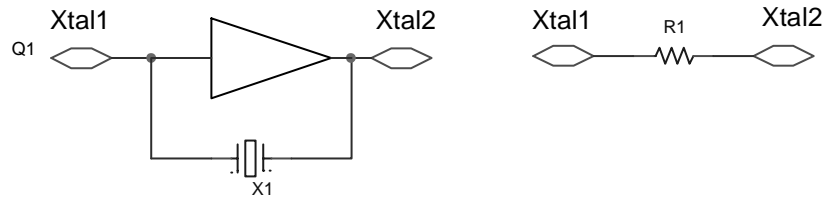
Series and Parallel Oscillators

series resonant oscillator

Some oscillator architectures force the crystal to operate around the series frequency and some others to work around the parallel frequency. This section gives information about these working modes.

This structure used a non inverted amplifier to force oscillation at its the natural series resonant frequency f_s . The crystal phase is zero, the resistance is minimum (R_1) and the current flow is maximum.

Figure 11. Series Resonant Structure

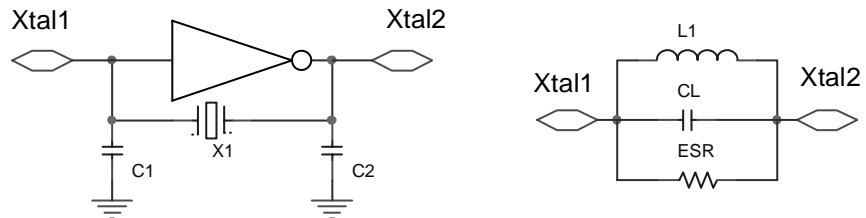


The feedback (X1) filters the oscillation frequency and send this signal in phase to Q1 input.

Parallel Resonant Oscillator

This structure used an inverted amplifier to force oscillation between f_s and f_a resonance frequencies where the crystal impedance appears inductive (L_1). This structure is called Pierce. To have this frequency resonant, f_p , the imaginary part of the crystal impedance must be zero. So only capacitive reactance can cancel the inductive one. This is why the C_1 and C_2 capacitors are added on $Xtal1$ and $Xtal2$ (see Figure 12).

Figure 12. Parallel Resonant Structure



The resonance frequency is given hereafter:

$$f_p := f_s \cdot \left[1 + \frac{C_1}{2 \cdot (C_0 + C_L)} \right]$$

where C_L is the capacitive load equivalent to the C_1 in parallel to C_2 .

The equivalent series resistance (ESR) is a little higher than for f_s and is given with the next expression:

$$ESR = R_1 \times \left(1 + \frac{C_0}{C_L} \right)^2, C_L = \frac{C_1 \times C_2}{C_1 + C_2}$$

Considering the expression of f_p , C_L plays an important role to have the required oscillation frequency. C_L is the loading capacitor used during the crystal calibration by the crystal manufacturer to tune the oscillator frequency. If an accurate frequency is

required **CL** must be respected. Here are some standard values are 13, 20, 24,30, and 32 pF.

Analysis Method

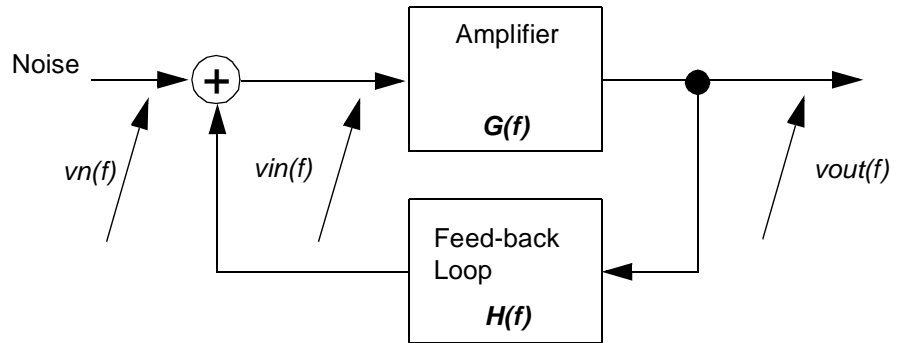
Two methods of oscillator analysis are considered in this application note. One method involves the open-loop gain and phase response versus frequency. A second method considers the amplifier as a one-port with negative real impedance to which the filter is attached. The second one will be preferred for very low frequency (32KHz).

The next sections explains the basics of these two methods and how to use them.

Open-loop Gain and Phase

This first method analyzes the product of the gain of the amplifier and the feed-back loop.

Figure 13. Basic Oscillator Architecture



The general equation to start-up the oscillation process is shown hereafter. Let's express $v_{out}(f)$:

$$v_{out}(f) = G(f) \times H(f) \times v_{out}(f) + G(f) \times v_n(f)$$

the transfer function between $v_{out}(f)$ and $v_n(f)$ is:

$$\frac{v_{out}(f)}{v_n(f)} = \frac{G(f)}{1 - G(f) \times H(f)}$$

the start-up condition can now be evaluated with the Barkhausen criteria:

$$|G(f) \times H(f)| > 1$$

$$\Phi(G(f) \times H(f)) = 0$$

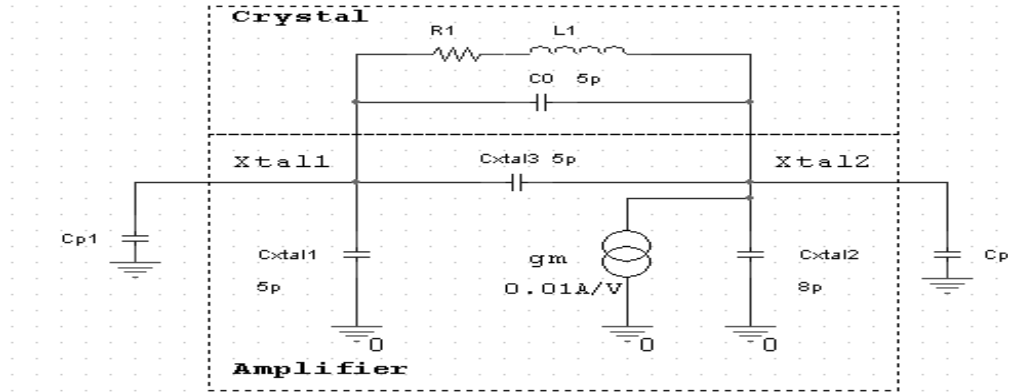
and lock condition can be expressed:

$$|G(f) \times H(f)| = 1$$

This start-up condition depends on the product of the gain and feed-back but also on the frequency. The lock condition is controlled by the non-linear area of the amplifier output. The gain is automatically reduced while the output oscillation increased until a stabilization point is found.

To analyze the oscillation conditions, it is useful to use a Spice simulator. Some free-ware are available on the Web and only the basic functions of Spice are required. Figure 14 shows a typical oscillator Spice circuit use to demonstrate the AC small signal analysis.

Figure 14. Typical crystal oscillator structure.



As seen previously, the open-loop gain is analyzed to check the oscillation conditions. To do that the feed-back loop is broken. The crystal has to be loaded with the same impedance than the input impedance of the amplifier.

Figure 15 shows the Spice circuit used to analyses the oscillation conditions. A 16MHz crystal is used for this analysis and **CP1** and **CP2** are tuned to have the oscillation conditions ($G > 0\text{dB}$, $\text{Phase}=0$).

Figure 15. Spice Circuit Used to Analyze the Oscillation Conditions

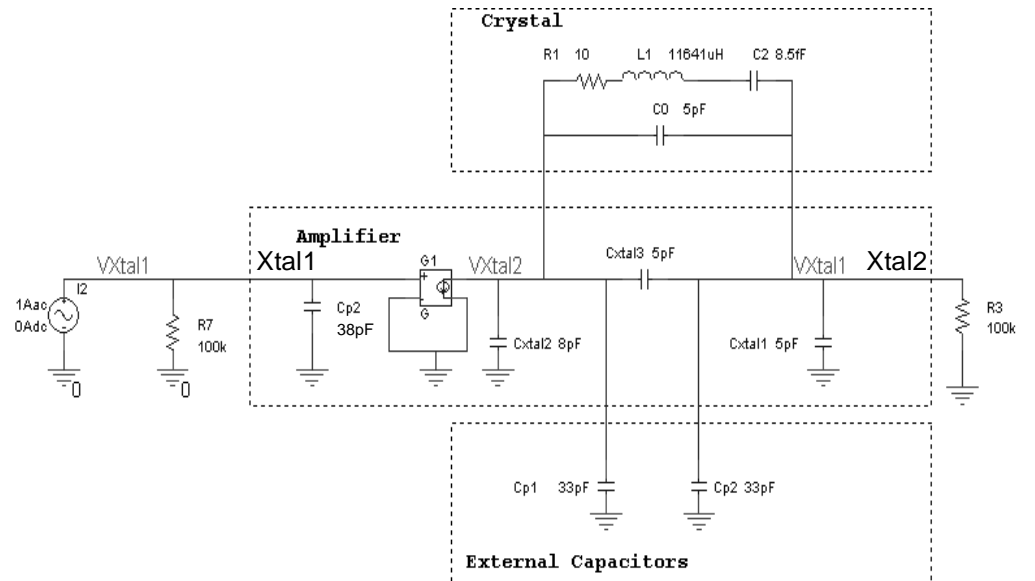
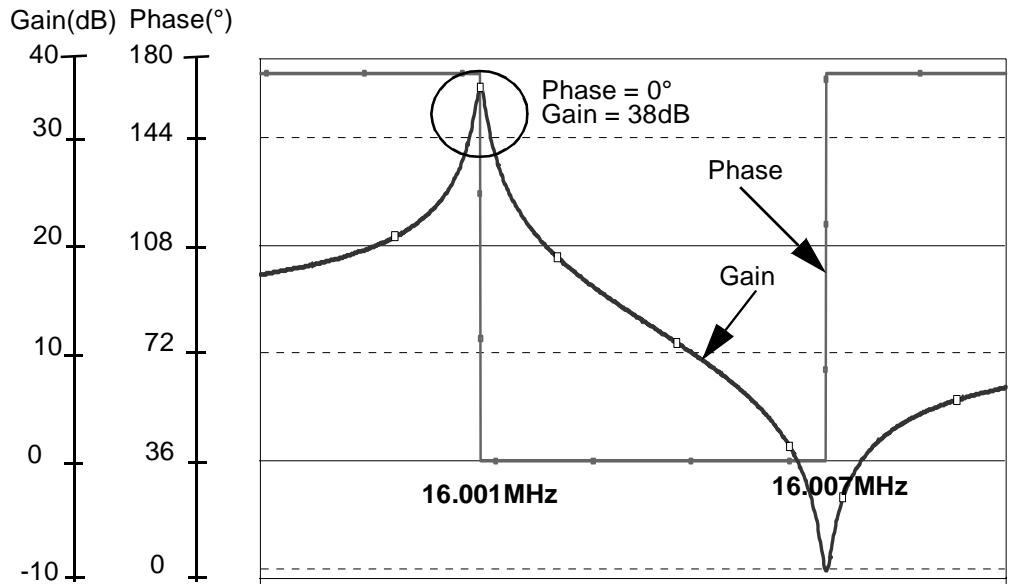


Figure 16 plots the gain and the phase of the open-loop circuit. At 16.001MHZ the gain is greater than unity (38dB) and the phase is zero. The oscillation conditions are met ensuring a good oscillator startup.

Figure 16. Gain and Phase response for the open-loop gain.

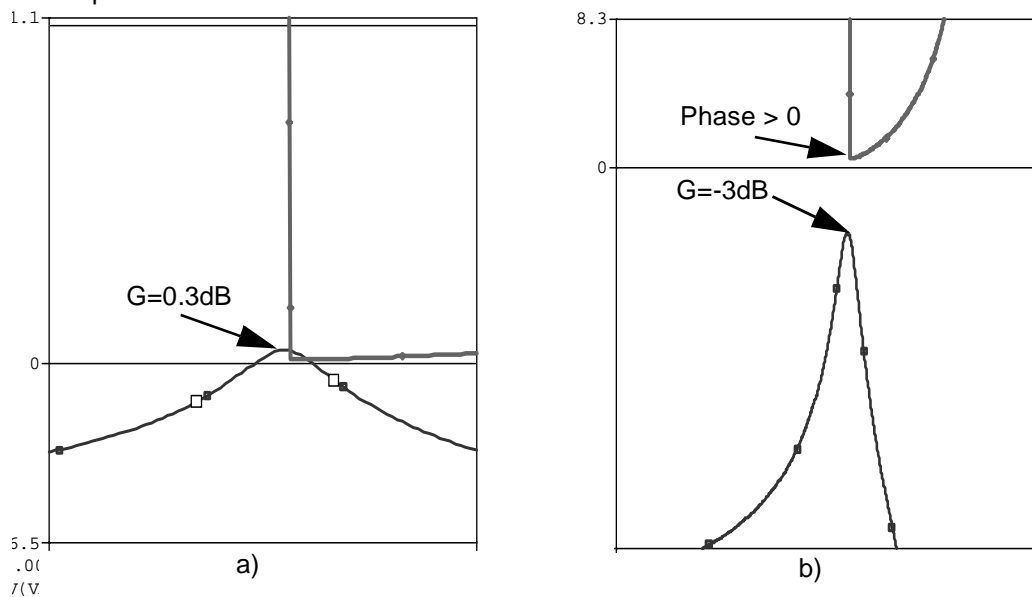


This method allows to check the maximum capacitive loads and the maximum electrical characteristics of the crystal.

Figure 17 (a) plots the gain and phase when **Cp1** and **CP2** are too big. The gain is now too small to guarantee a proper startup. The phase begins to shift and is no longer zero.

Figure 17 (b) plots the gain and phase when the equivalent resistance of the crystal (**R1**) is too big. The gain is now negative and the phase is not zero. The oscillation conditions are not met and this oscillator will not start.

Figure 17. Gain and phase for two conditions



a) **Cp1** and **Cp2** are too big (56pF), b) **R1** is too big = 40ohms.

Table 3 resumes the case studies analyze with the spice model and tool.

Table 3. Oscillation Conditions versus Cp1, Cp2 and R1

Cp1(pF)	Cp2(pF)	R1(ohms)	Oscillation Conditions
33	33	10	Yes
33	33	40	No
56	56	10	No

CP1 and CP2 are generally chosen to be equal maintaining a gain in closed loop equal to the unity.

Negative feed-back resistance

The second method analyzes the real part on the input impedance of the amplifier and compares it with the real part of the pass-band filter. The impedance seen on the input amplifier is negative under certain conditions and cancelled the crystal resistance. In that case there is no more lost of energy and oscillations are stabilized.

Figure 18 shows the equivalent model of an oscillator. The crystal is equivalent to a RLC filter corresponding to the motional arm. **Z3** in the equivalent impedance across **Xtal1** and **Xtal2** pins including the **C0** crystal capacitor and **Cx3**. **Z1** and **Z2** are the input and output impedances including the two external capacitors **Cp1** and **Cp2** used to adjust the oscillator operating point.

Figure 18. a) Oscillator Equivalent model b) Equivalent model around the resonance.

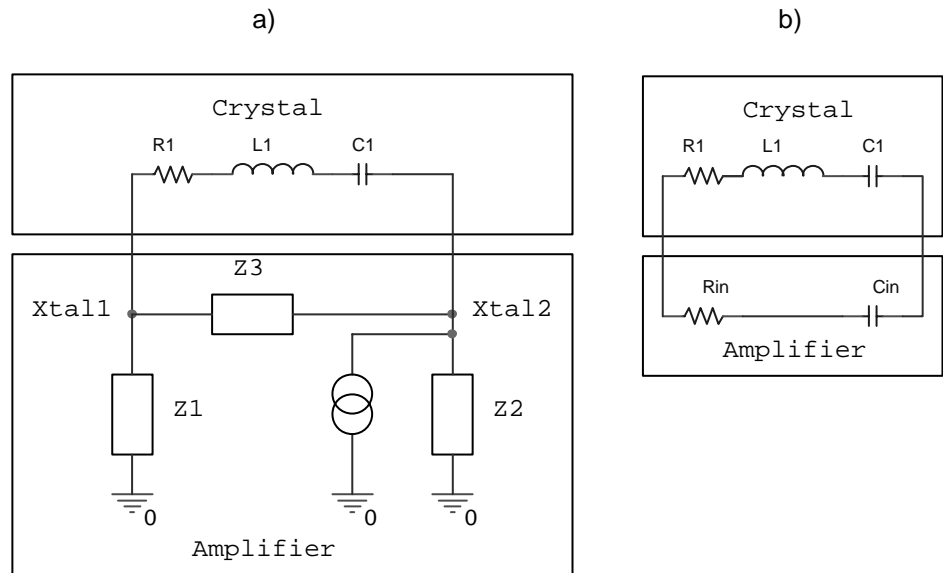


Figure 18 shows in what conditions the oscillator will oscillate. To have an oscillation stable in steady condition, the lost of energy in the crystal has to be cancelled. This condition occurs when:

$$R_{in} = -R1$$

and at the frequency:

$$f = \frac{1}{6,28 \times \sqrt{L1 \times \frac{C1 \times C_{in}}{C1 + C_{in}}}}$$

C_{in} is the equivalent capacitor seen between Xtal1 and Xtal2 and is equal to:

$$C_{in} = C0 + Cx3 + \frac{Cx1 \times Cx2}{Cx1 + Cx2}$$

where **Cx1 and Cx2** are the global capacitors seen on the input and output pins. **Cx3** is the capacitor seen between **Xtal1** and **Xtal2** pins.

To ensure a good startup of the oscillator, **Cx1** and **Cx2** have to be correctly adjusted. In order to define them, the amplifier impedance must respect the conditions on **R_{in}** and **C_{in}** parameters:

- **R_{in}: Cx1 and Cx2** has to be adjusted to have **R_{in} > R1**:

$$R_{in}(Zc) = \frac{(Cx1 \times Cx2) \times -gm}{(gm \times Cx3)^2 + \omega^2 \times (Cx1 \times Cx2 + Cx2 \times Cx3 + Cx1 \times Cx3)^2}$$

- **C_{in}: Cx1 and Cx2** have to be adjusted to obtain a negative imaginary part and finally a input capacitor.

$$Im(Zc) = \frac{-gm^2 \times Cx3 + \omega^2 \times (Cx1 + Cx2) \times (Cx1 \times Cx2 + Cx1 \times Cx3 + Cx2 \times Cx3)^2}{\omega \times ((gm \times Cx3)^2 + \omega^2 \times (Cx1 \times Cx2 + Cx2 \times Cx3 + Cx1 \times Cx3)^2)}$$

$$C = \frac{Im(Zc)}{6,28 \times f}$$

gm is the amplifier gain.

An example is given hereafter. The main characteristics of this case study is:

- **Amplifier:** gm=0.01A/V, Cxtal1=5pf, Cxtal2=8pF, Cxtal3=5pf
- **Crystal:** R1=80, L1=11.64mH, C1=8.5fF, C0=5pF

Figure 19. Oscillator Example

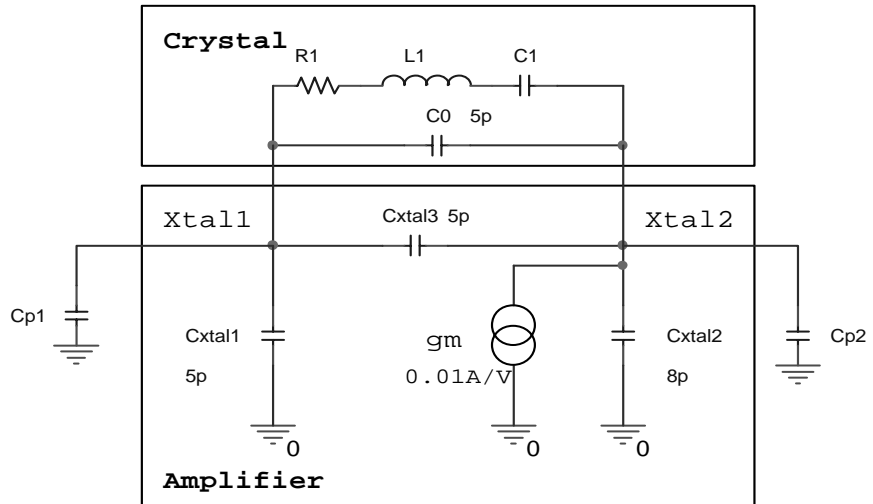


Table 4 shows two cases: first, there is no external additional capacitors and second two capacitors are adjusted to the oscillation frequency.

When there is no capacitor R_{in} is less than $R1$ (80 ohms) and no oscillation occurs.

With $Cp1=Cp2=5pf$, R_{in} is -175 ohms and is greater than $R1$ and the condition to have oscillations is met. As with the previous method, $Cp1$ and $Cp2$ can be tuned and the electrical characteristics can be checked. Table 4 resumes the case studies.

Table 4. $Cp1$ and $Cp2$ capacitors with $R1=80ohms$.

$Cp1(pF)$	$Cp2(pF)$	$R_{in}(ohms)$	$C_{in}(pF)$	Oscillation Condition
0	0	-60	8.26	No
5	5	-175	9.2	Yes

Conclusions

Two methods have been presented to analyze and to check the oscillation conditions. They have shown the possibility to predict the added capacitors in versus the electrical characteristics of the crystal or resonator devices. It will help to specify the margin of the crystal and resonator devices.



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